# Automata and Formal Languages <br> Homework Set 2 <br> September 24, 2002 <br> shieng@ncnu.edu.tw 

Due date: Oct. 1

## Problem 1

1.1 The following are the state diagrams of two DFAs, $M_{1}$ and $M_{2}$. Answer the following questions about these machines.

a. What is the start state of $M_{1}$ ?
b. What is the set of accept states of $M_{1}$ ?
c. What is the start state of $M_{2}$ ?
d. What is the set of accept states of $M_{2}$ ?
e. What sequence of states does $M_{1}$ go through on input aabb?
f. Does $M_{1}$ accept the string aabb?
g. Does $M_{2}$ accept the string $\varepsilon$ ?

## Problem 2

Give the formal description of the machines $M_{1}$ and $M_{2}$ pictured in Problem 1.

## Problem 3

1.3 The formal description of a DFA $M$ is $\left(\left\{q_{1}, q_{2}, q_{3}, q_{4}, q_{5}\right\},\{\mathrm{u}, \mathrm{d}\}, \delta, q_{3},\left\{q_{3}\right\}\right)$, where $\delta$ is given by the following table. Give the state diagram of this machine.

|  | u | d |
| :---: | :---: | :---: |
| $q_{1}$ | $q_{1}$ | $q_{2}$ |
| $q_{2}$ | $q_{1}$ | $q_{3}$ |
| $q_{3}$ | $q_{2}$ | $q_{4}$ |
| $q_{4}$ | $q_{3}$ | $q_{5}$ |
| $q_{5}$ | $q_{4}$ | $q_{5}$ |

## Problem 4

Give state diagrams of DFAs recognizing the following languages. In all cases the alphabet is $\{0,1\}$.

1. $\{w \mid w$ begins with a 1 and ends with a 0$\}$.
2. $\{w \mid w$ contains at least three 1 s$\}$.
